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# Ion – ion recombination in $SF_6$ and in $SF_6 - C_2H_6$ mixtures for high values of E/N

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Abstract. Ion-ion recombination coefficients in a decaying  $SF_6$  plasma and in  $SF_6-C_2H_6$  mixtures are measured in the pressure range 15–90 Torr for reduced field strengths 100–250 Td. The charge composition is analysed and dominating ion-ion recombination channels in such plasmas are determined. Relations for estimating the potential drop at the electrodes are obtained for decaying plasma in strongly electronegative gases. The results of measurements are extrapolated for estimating the ion-ion recombination coefficient in  $SF_6$  for nearly critical field strengths. It is concluded that the ion-ion recombination should be taken into account in calculations of the discharge characteristics in non-chain reaction HF lasers.

*Keywords*:  $SF_6$ , ion-ion recombination, HF laser, electronegative gases.

#### 1. Introduction

The possibility of exciting a self-sustained volume discharge (SVD) without preionisation, i.e., self-initiated volume discharge [1] in SF<sub>6</sub> mixtures with hydrocarbons, was discovered in Ref. [2], and raised the problem of scaling nonchain reaction HF lasers to a qualitatively new level, increasing their power and energy by more than an order of magnitude (by a factor of 40). At present, the energy emitted by SVD-initiated non-chain reaction HF lasers exceeds 400 J for an electrical efficiency of more than 4 % [3].

In this connection, it is interesting to continue the investigation of SVD in  $SF_6$  and in mixtures of  $SF_6$  with hydrocarbons. Because of its strongly electronegative nature, the  $SF_6$  plasma of such a discharge possesses a number of specific features. For example, the concentration of positive and negative ions in such a plasma is much higher than the electron concentration (by almost two orders of magnitude) [1, 4]. For this reason, processes associated with the ionic component of plasma (destruction of negative ions by

Received 12 March 2001 *Kvantovaya Elektronika* **31** (7) 629–633 (2001) Translated by Ram Wadhwa electron impact, dissociative electron-ion recombination and ion-ion recombination) may play a significant role in the discharge kinetics [4]. The latter process affects considerably the ion concentration in SVD and completely determines the charge kinetics in a decaying plasma.

The ion–ion recombination in SF<sub>6</sub> and its mixtures with hydrocarbons in an external electric field has not been adequately studied. Apparently, only two works [5, 6] reported the measurement of the ion–ion recombination coefficient  $\beta$ in SF<sub>6</sub>, binary mixtures of SF<sub>6</sub> with the hydrocarbon CH<sub>4</sub> used rarely in HF lasers, and in ternary SF<sub>6</sub>–CH<sub>4</sub>–Ar/He mixtures at working pressures p > 100 Torr and relatively low reduced electric field strengths E/N < 160 Td (N is the concentration of neutral particles). The remaining experimental [7] and theoretical (simulation by the Monte Carlo method) [8] studies cover a much wider range of pres-sures ( $\sim 10^2 - 10^4$  Torr), however, in the zero electric field approximation.

To calculate the SVD characteristics in a non-chain reaction HF laser, of main interest is the coefficient  $\beta$  for mixtures of SF<sub>6</sub> with the hydrocarbon C<sub>2</sub>H<sub>6</sub> [1-3] for p = 30 - 90 Torr (lasers with quite large apertures) and values of E/N close to the critical value  $(E/N)_{\rm cr}$  in SF<sub>6</sub>. The aim of this paper is to measure the ion – ion recombination coefficient in pure SF<sub>6</sub> and its mixtures with C<sub>2</sub>H<sub>6</sub> in the above-mentioned pressure range for values of E/N up to 250 Td. In particular, this makes it possible to obtain a reasonable value of the coefficient  $\beta$  for  $E/N \sim (E/N)_{\rm cr}$ characteristic of the self-sustained discharge.

## 2. Experimental

Ion plasma for measuring the coefficient  $\beta$  was induced by a pulsed SVD. The scheme of the experimental setup is shown in Fig. 1. The SVD was ignited between an anisotropically resistive cathode K of size 5 cm × 5 cm (similar to the one used in Ref. [9]) and a disc-shaped anode A of diameter 12 cm, rounded off at the edge to a radius 1 cm, by commutating the voltage with a gap P1. The interelectrode distance was varied from 2 to 8 cm. The anisotropically resistive cathode made it possible to obtain a discharge distributed uniformly over the cathode surface, which is necessary for the applicability of comparatively simpler relations that we will use below for determining ion concentration.

The resistance  $R_c \sim 1 \Omega$  of the anisotropically resistive cathode is much smaller than the resistance  $R_p \sim 1 \ k\Omega$  of the ion plasma, and hence does not introduce any noticeable distortions in the measured values of ion current. The capacitance 2–8 nF of capacitor  $C_1$  was determined from the

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Figure 1. Scheme of the setup for measuring the ion – ion recombination coefficient.

conditions of the SVD stability and homogeneity. The capacitor  $C_2 = 174$  nF connected to the gap P2 was used to mantain a constant voltage across the discharge gap during the measurement of the ion current (up to 20 µs). The resistance  $R_2 = 50 \Omega$ , connected in the discharge circuit of this capacitor, minimises its influence on the energy released in the SVD plasma. The gap P2 was triggered automatically upon activation of the gap P1 and closure of the capacitor  $C_3$  circuit through the resistor  $R_3$ . The current was detected by the shunt resistance  $R_{\rm sh}$ .

Because the ion current of the decaying plasma was much weaker (by several orders of magnitude) than the maximum SVD current, to improve the accuracy of measurements, the signal from the shunt was cut off at the level of 1 V by the  $R_1 - D$  diode limiter. Calibration of the ion current measuring circuit and verification of its linearity were performed by shunting a capacitor (through the gap) charged to a voltage ~ 4 kV through a resistance ~ 1 k $\Omega$ . Fig. 2a shows typical oscillograms of the current and voltage across the discharge gap recorded in this way. The negative spikes on the oscillograms correspond to the SVD current and voltage.

The ion-ion recombination coefficient  $\beta$  was calculated from the current oscillogram I(t) for a fixed voltage U across the discharge gap with the help of the relations

$$n_{\rm i}(t) = \frac{I(t)}{Se(b_{\rm i}^+ + b_{\rm i}^-)E},$$
(1)

$$n_{\rm i}(t) = \frac{n_{\rm i}(0)}{1 + n_{\rm i}(0)\beta t}.$$
(2)

Here,  $n_i(t)$  is the ion concentration; *S* is the cathode area; *e* is the electron charge; E = U/d;  $n_i(0)$  is the initial ion concentration. Relations (1) and (2) are written under the assumption that there are only one type of positive and one type of negative ions with mobilities  $b_i^+$  and  $b_i^-$ , respectively. The possibility of such an assumption is discussed below. The quantities  $n_i(0)$  and  $\beta$  were determined from relation (2) from the values of  $n_i(t)$  reconstructed from (1) by the method of least squares (Fig. 2b).

## 3. Results of measurements

Fig. 3 shows the dependences of the ion-ion recombination coefficient  $\beta$  on the parameter E/N in pure SF<sub>6</sub> under a pressure p = 15 - 90 Torr. One can see that  $\beta$  strongly decreases with increasing E/N over the entire pressure range. This result is consistent with the data presented in Ref. [5], where measurements were performed by the



**Figure 2.** (a) Oscillograms of voltage U across the discharge gap (upper trace) and the current I in a decaying plasma (lower trace), and (b) dependence of the ion concentration  $n_i$  on time t, calculated from the oscillograms of Fig. 2a (dark circles) and by the method of least squares (solid curve) for p = 30 Torr and E/N = 230 Td.

standard technique using an electron beam for producing the ion plasma. In the region of small E/N, the coefficient  $\beta$ increases with pressure p almost linearly. In the range E/N > 200 Td, this law is violated and the dependence of  $\beta$ on p becomes weaker. This fact does not contradict the results obtained in Ref. [10], where it was shown by calculations that the ion-ion recombination coefficient depends not only on the parameter E/N, but also on the absolute value of the electric field strength E, decreasing with increasing E.



**Figure 3.** Dependences of the ion–ion recombination coefficient  $\beta$  on the parameter E/N for SF<sub>6</sub> under different pressures.

Note also that in the region of low values of E/N = 100 - 160 Td, the values of the coefficient  $\beta$  measured in our experiments for p = 90 Torr are close to the corresponding values from Ref. [5]. In the SF<sub>6</sub>:C<sub>2</sub>H<sub>6</sub> = 10:1 mixture, the values of  $\beta$  obtained for E/N = 250 Td and p = 60 and 90 Torr are  $4.3 \times 10^{-8}$  and  $6.5 \times 10^{-8}$  cm<sup>3</sup> s<sup>-1</sup>, respectively. No changes  $\beta$  were observed upon variation of the SVD parameters, such as the specific deposited energy and the discharge-current duration over a rather wide range.

#### 4. Discussion of results

Consider the ion composition and the nature of ion-ion recombination in  $SF_6$  and its mixtures with  $C_2H_6$ . We are not aware of any experimental facts confirming the presence of positive  $SF_6^+$  ions in the plasma of self-sustained discharge in  $SF_6$ . According to the results of direct mass-spectrometric measurements (see, for example, Refs [11, 12]), the  $SF_5^+$  ion dominates in the plasma. This is consistent with the results presented in paper [13], in which it was shown that the  $SF_6^+$  ion formed in the plasma is in predissociative state and dissociates into the  $SF_5^+$  ion during a time period much smaller than any characteristic discharge times. As for the negative ions, several kinds of such ions should be considered in general.

In the range of values of E/N close to  $(E/N)_{cr}$  and below, in which we are interested, the dissociative attachment of electrons to SF<sub>6</sub> molecules results in the formation of predominantly negative SF<sub>6</sub><sup>-</sup> ions [14]. The rates of generation of the SF<sub>5</sub><sup>-</sup> and  $F^-$  ions are about half the rate of formation of SF<sub>6</sub><sup>-</sup> ions [14]. The mobilities of the SF<sub>6</sub><sup>-</sup> and SF<sub>5</sub><sup>-</sup> ions are virtually identical and are close to those obtained in the Langevin (polarisation) approximation [13]. The mobility of the  $F^-$  ions can also be estimated quite accurately in the same approximation.

The dissociative charge exchange of the  $SF_6^-$  and  $SF_5^$ ions with  $SF_6$  molecules, resulting in the formation of negative ions of another kind (mainly  $F^-$  ions) does not have time to occur even under the maximum pressures ~ 90 Torr used in our experiments. For example, according to the data presented in Ref. [15], the minimum time  $\tau_{min}$  for the reaction  $SF_6^- + SF_6 \rightarrow SF_6 + SF_5 + F^-$  at p = 90 Torr and for  $E/N \sim (E/N)_{cr}$  corresponding to the self-sustained discharge stage exceeds 1 µs, while the duration of the SVD itself in these experiments is ~ 100 – 300 ns.

In a decaying plasma with much smaller values of the ratio E/N, the time  $\tau_{\min}$  increases by several orders of magnitude. Thus, the SF<sub>6</sub><sup>-</sup> and SF<sub>5</sub><sup>-</sup> ions vanish in the decaying SF<sub>6</sub> plasma only as a result of recombination with the SF<sub>5</sub><sup>+</sup> ions. The detachment of an electron from the F<sup>-</sup> ion can occur only in the layers in the vicinity of the electrode (see below). As a result, the decrease in the concentration of F<sup>-</sup> ions in the plasma is also determined only by their recombination with SF<sub>5</sub><sup>+</sup> ions.

In the pressure range under study, a three-body mechanism of ion-ion recombination is realised. According to the preliminary estimates obtained by using the well-known three-body recombination models [16] and assuming the polarisation nature of interaction of ions with gas molecules, it can be expected that the coefficients of recombination of  $SF_6^-$  and  $SF_5^-$  ions with  $SF_5^+$  ions are close, while the coefficients of recombination of  $F^-$  and  $SF_5^+$  ions are much higher. In this connection, we consider a decaying ion plasma with one type of positive ions with the concentration  $n^+(t)$  and two types of negative ions with concentrations  $n_1^-(t) \bowtie n_2^-(t)$ .

Suppose that the ion–ion recombination coefficients are equal to  $\beta_1$  and  $\beta_2$ , respectively. For the sake of definiteness, we assume that  $\beta_2 > \beta_1$ . Taking into account the quasi-neutrality of the plasma, we obtain the following integro-differential equation for the density of positive ions:

$$\frac{\mathrm{d}\varphi}{\mathrm{d}\tau} = q_1 \exp(-\varphi) + q_2 \exp(-\sigma\varphi),$$

$$\varphi = \int_0^\tau y \,\mathrm{d}\tau, \ y = \frac{n^+(t)}{n^+(0)},$$
(3)

$$\tau = \beta_1 n_1^-(0)t, \ \sigma = \frac{\beta_2}{\beta_1}, \ q_1 = \frac{n_1(0)}{n^+(0)}, \ q_2 = \frac{n_2(0)}{n^+(0)}.$$

Here,  $n^+(0)$ ,  $n_1^-(0)$  and  $n_2^-(0)$  are the initial concentrations of positive and negative ions.

Because  $\sigma > 1$  and  $\varphi(\tau) \to \infty$  for  $\tau \to \infty$ , the second term in Eqn (3) can be neglected starting from a certain instant of time. Taking into account that  $n_1^-(t) = n_1^-(0)$  $\times \exp(-\varphi)$ , this equation is transformed into the recombination equation only for negative ions with the smaller recombination coefficient  $\beta_1$ . As applied to the SF<sub>6</sub> plasma, this means that within a certain time interval after the recombination onset, negative ions  $SF_6^-$  and  $SF_5^-$ , which have close values of the mobility and recombination coefficient (see above), start dominating in the plasma along with the positive  $SF_5^+$  ions. This justifies the use of Eqns (1) and (2). This is clearly shown in Fig. 2b. One can see that for t > 8 $\mu$ s, the time decay  $n_i(t)$  of the ion concentration calculated from (1) strictly follows the recombination relation (2). The values of ion mobilities used in calculations were borrowed from Ref. [13].

The complex SF<sub>6</sub><sup>-</sup>(SF<sub>6</sub>) ion was considered as the main negative ion in Refs [5, 6, 8], but the gas pressures were 5– 10 times higher in these works than in our experiments. Taking into account that the rate of clusterisation of the SF<sub>6</sub><sup>-</sup> ions quadratically depends on *p*, we can expect that the fraction of the complex SF<sub>6</sub><sup>-</sup>(SF<sub>6</sub>) ions in the investigated plasma is insignificant. Moreover, according to Ref. [13], the mobilities of ions SF<sub>6</sub><sup>-</sup> and SF<sub>6</sub><sup>-</sup>(SF<sub>6</sub>) differ by just a few percent in the range  $E/N \sim 100 - 250$  Td, so that the formation of complex ions under the conditions of our experiments is insignificant at all.

In addition to the SF<sub>5</sub><sup>+</sup> ions, the SF<sub>6</sub>: $C_2H_6 = 10:1$ mixture also contains positive ions formed upon the electron impact ionisation of  $C_2H_6$ . According to Refs [17, 18], the mechanism of dissociative ionisation with the formation of  $C_2H_4^+$  ions and  $H_2$  molecules dominates in this case. Using the Langevin approximation and the Blank law [19], we find that the mobility of  $SF_5^+$  and  $C_2H_4^+$  ions in the  $SF_6:C_2H_6 =$ 10:1 mixture is determined by their interaction with the  $SF_6$ molecules. Despite the fact that the mobility of  $C_2H_4^+$  ions (estimated in the polarisation limit) is about 1.8 times higher than the mobility of  $SF_5^+$  ions, the  $C_2H_4^+$  ions do not make a significant contribution to the total current I(t) for the above-mentioned ratio of the concentrations of SF<sub>6</sub> and C<sub>2</sub>H<sub>6</sub>. As a result, the set of negative ions remains unchanged. Taking into account that positive  $SF_5^+$  ions dominate in the plasma under study, expression (2) describing the recombination kinetics remains applicable for the mixture as well.

While the formation of positive ions in the  $SF_6 - C_2H_6$ mixture is also possible upon the charge exchange of the  $SF_5^+$  ions with the  $C_2H_6$  molecules (although, in our opinion, the situation is not quite clear), estimates show that the charge exchange times are  $\sim 10^{-8} - 10^{-7}$  s even for the lowest  $C_2H_6$  concentrations of  $\sim 10^{17}$  cm<sup>-3</sup>. Therefore, only one positive ion will dominate on the time scale exceeding 1 µs of interest to us.

The polarisation approximation was used several times while estimating the ion mobility, although this cannot be always substantiated rigorously under the conditions of our analysis. However, it is known that, as a rule, the values of mobility obtained by using the Langevin formula do not differ significantly from the measured values. This is clearly demonstrated in Ref. [13] for the  $SF_6$  molecules. Thus, the above arguments concerning the ion composition of the working medium and the nature of ion recombination under the investigated conditions are justified, at least in principle. The above-mentioned constancy of the ion-ion recombination coefficient upon a considerable variation of the discharge parameters is another indirect evidence in favour of this conclusion, since it follows from what has been stated above that the set of negative ions in the recombination plasma depends weakly on the initial discharge conditions.

The field strength  $E_p$  in the plasma was determined in our experiments by dividing the voltage across the discharge gap by the interelectrode distance. It is well known, however, that the voltage drop at the electrode may be very high in the case of strongly electronegative gases. Therefore, it should be interesting to estimate the error introduced in the value of  $E_p$  by this method.

To estimate the voltage drop  $U_{\rm c}$  across the cathode, we will use the one-dimensional approximation and assume as in Ref. [20], that the field  $E_c(x)$  in the cathode layer is independent of the longitudinal coordinate x, i.e.,  $E_{\rm c}(x) = E_{\rm c}$ . The estimates made below show that under the conditions under study, this quantity greatly exceeds not only  $E_{\rm p}$ , but also the critical field strength  $E_{\rm cr}$ , so that the formation of negative ions in the layer can be neglected. In this case, the distributions of the current density  $j_e(x)$  of electrons and  $j_{\pm}(x)$  of positive ions in the cathode region are described by the same equations as in the case of an electropositive gas. Beyond the cathode layer  $(x > d_c)$ , the electron component of the total current density  $J_t$  in a decaying plasma rapidly vanishes because of an intense attachment of electrons. As a result, the boundary conditions are somewhat different from those considered normally for the electropositive gas:

$$j_{\rm e}(0) = \gamma j_+(0), \ \ j_{\rm e}(d_{\rm c}) + j_+(d_{\rm c}) = J_{\rm t},$$
(4)

where  $\gamma$  is the secondary electron emission coefficient. The second condition in (4) can also be formulated as  $j_e(d_c) = j_-(d_c)$ , where  $j_-(x)$  is the current density of negative ions. Using the standard technique (see, for example, Ref. [20]), the continuity equations for  $j_e(x) \equiv j_+(x)$  taking into account Eqns (4) and the fact that  $\gamma \ll 1$ , we can easily obtain the following expression in the reduced variables accepted in the theory of near-electrode layers [21]:

$$\frac{\alpha(E_{\rm c}/p)}{p}pd_{\rm c} = B_1, \ B_1 = \ln\left(\frac{1+\gamma}{\gamma}\frac{b_{\rm i}^-}{b_{\rm i}^+ + b_{\rm i}^-}\right),\tag{5}$$

where  $\alpha$  is the Townsend coefficient.

Proceeding from the Poisson equation, we obtain a relation between parameters  $E_c$  and  $d_c$  [20]:

$$\left(\frac{E_{\rm c}}{p}\right)^2 = \frac{(J_{\rm t}/p^2)pd_{\rm c}}{\varepsilon_0 b_{\rm i}^+ p},\tag{6}$$

where  $\varepsilon_0$  is the dielectric constant of vacuum. Then, we obtain from Eqns (5) and (6) the following relations for determining  $U_c$ :

$$\frac{(E_{\rm c}/p)^2 [\alpha(E_{\rm c}/p)/p] \varepsilon_0 b_{\rm i}^+ p}{J_{\rm t}/p^2} = B_1, \quad U_{\rm c} = \frac{E_{\rm c}}{p} p d_{\rm c}.$$
 (7)

To estimate the potential drop in the anode region, we should consider impact ionisation as well as the formation and neutralisation of negative ions The latter process leads to the emergence of seed electrons in the anode region because the electron current coming to this region from the decaying plasma is vanishingly small. In analogy with the above conclusion, we assume that the field  $E_a$  in the anode layer is constant.

In the approximation of a planar layer, the system of corresponding continuity equations can be written in the form

$$\frac{\mathrm{d}j_{\mathrm{e}}(x)}{\mathrm{d}x} = -\alpha j_{\mathrm{e}}(x) - \delta j_{-}(x), \quad \frac{\mathrm{d}j_{-}(x)}{\mathrm{d}x} = -\eta j_{\mathrm{e}}(x) + \delta j_{-}(x),$$

$$\frac{\mathrm{d}j_{+}(x)}{\mathrm{d}x} = \alpha j_{\mathrm{e}}(x).$$
(8)

Here,  $\eta$  is the electron attachment coefficient;  $\delta$  is the coefficient of detachment of electrons from negative ions in collisions with gas molecules. The coordinate *x* is measured from the anode (*x* = 0) into the depth of the discharge gap.

The decrease in the electron current caused by the attachment to the SF<sub>6</sub> molecules can be neglected for the same reason as in the case of the cathode layer ( $E_a \ge E_{cr}$ ). Taking this into account, the boundary conditions at the anode and at the boundary between the anode layer and the plasma ( $x = d_a$ ) have the form

$$j_{+}(0) = 0, \ j_{e}(d_{a}) = 0, \ j_{-}(d_{a}) + j_{+}(d_{a}) = J_{t}.$$
 (9)

As a result, we arrive at the relation

$$\begin{aligned} &(\lambda_1 + \lambda_2)d_{\rm a} = B_2, \\ &B_2 = \ln\left\{\frac{b_{\rm i}^+}{b_{\rm i}^-}\frac{\lambda_2}{\lambda_1} + \left[1 + (\lambda_1 + \lambda_2)d_{\rm a}\right]\frac{b_{\rm i}^+ + b_{\rm i}^-}{b_{\rm i}^-}\right\}, \end{aligned} \tag{10}$$

where  $\lambda_{1,2} = \{\pm (\delta - \alpha) + [(\alpha - \delta)^2 + 4\alpha \delta]^{1/2}\}/2$ . Since  $E_a \gg E_{cr}$ , we have  $\alpha \gg \delta$ ,  $\lambda_1 \simeq \delta$ ,  $\lambda_2 \simeq \alpha$  and expression (10) is considerably simplified:

$$\frac{\alpha(E_{\rm a}/p)}{p}pd_{\rm a} \approx \ln\left[\frac{\alpha(E_{\rm a}/p)}{\delta(E_{\rm a}/p)}\right].$$
(11)

Using a relation between  $E_a$  and  $d_a$  analogous to (6), and neglecting the difference in the mobilities of positive and negative ions  $(b_i^+ \approx b_i^- \approx b_i)$ , we obtain in the approximation  $\alpha \ge \delta$  the following expression for  $E_a$ :

$$\left(\frac{E_{\rm a}}{p}\right)^2 \frac{[\alpha(E_{\rm a}/p)/p]\varepsilon_0 b_{\rm i} p}{J_{\rm t}/p^2} \approx \ln\left[\frac{\alpha(E_{\rm a}/p)}{\delta(E_{\rm a}/p)}\right],\tag{12}$$

which is used, together with (11), for finding  $d_a$  and, hence, the potential drop  $U_a$  across the anode.

Using the results obtained, we can now easily estimate the relative error  $\xi = (E - E_p)/E$  in determining the field  $E_p$  in a decaying plasma:

$$\xi = \frac{B_1/\eta_{\rm c} + B_2/\eta_{\rm a}}{U}, \quad \eta_{\rm c,a}(E_{\rm c,a}/N) = \frac{k_{\rm i}(E_{\rm c,a}/N)}{u_{\rm e}(E_{\rm c,a}/N)(E_{\rm c,a}/N)},$$
(13)

where  $k_i(E_{c,a}/N)$  and  $u_e(E_{c,a}/N)$  are the impact ionisation constant and the drift velocity of electrons, respectively.

As an example, consider the SF<sub>6</sub> plasma under a pressure p = 30 Torr with a characteristic current density  $J_t \sim 1 \text{ A cm}^{-2}$ . Using the data of Refs [14, 15, 22] for  $k_i$  and  $u_e$  and expressions (7), (11), (12) and (13), we obtain  $\xi \approx 0.1$ . The same relative error is typical for all other plasma decay regimes considered in this work.

We have made a number of assumptions while estimating the quantities  $U_c$  and  $U_a$  (for example, the possibility of formation of double layers in the electrode region was also not considered). Nevertheless, the estimates obtained approximate well the real values. An indirect confirmation of this is provided, for example, by the fact that the estimates of the quantities  $\Delta U = U_c + U_a$  are in satisfactory agreement with the corresponding values obtained by us by extrapolating the experimental dependence  $U_{st}(pd)$  [1] for SF<sub>6</sub> and mixtures of SF<sub>6</sub> with C<sub>2</sub>H<sub>6</sub> in the region  $pd \rightarrow 0$ ( $U_{st}$  is the voltage in the quasi-stationary phase of the SVD).

The order of magnitude of the electrode layer relaxation time coincides with the drift time  $\tau_{c,a} = \varepsilon_0(E_{c,a}/p)/[(J_t/p^2)p]$ of ions through this layer. For example, we obtain  $\tau_{c,a} \sim 10^{-8}$  s for p = 30 Torr and  $J_t \sim 1$  A cm<sup>-2</sup>. Values of  $\tau_{c,a}$ of the same order of magnitude are also obtained under other conditions. Because we are interested only in the microsecond region in this work, the quasi-stationary approximation used above is fully justified.

For the characteristic values of  $E_c$  and  $E_a$  in the investigated gases under the conditions described above, the relation  $l_e \sim l$  is satisfied in the electrode regions, where l and  $l_e$ are the mean free path and the energy relaxation length of electrons, respectively. It also follows from relations (5), (6), (11) and (12) that  $d_{c,a} \gg l_i$ , where  $l_i$  is the ionisation length in the cathode or anode region. Taking into account that  $l/l_i$ < 1, we obtain  $l_e/d_{c,a} \ll 1$ . Therefore, local dependences of transport coefficients on the field strength can be used in the above description.

## 5. Conclusions

We have measured the ion-ion recombination coefficients in SF<sub>6</sub> and in SF<sub>6</sub>:C<sub>2</sub>H<sub>6</sub> = 10:1 mixtures in the pressure range 15-90 Torr for reduced electric field strengths E/N = 100 - 250 Td. The error in the estimates of fields in the plasma does not exceed 10 % for an overall measuring error below 20 %. The extrapolation of the results of measurements to the region of higher values of E/N provides an estimate  $10^{-8}$  cm<sup>3</sup> s<sup>-1</sup> for the coefficient of recombination  $\beta$  of the SF<sub>6</sub><sup>-</sup> and SF<sub>5</sub><sup>-</sup> ions with the SF<sub>5</sub><sup>+</sup> in SF<sub>6</sub> for  $E/N \sim (E/N)_{cr}$ . The values of  $\beta$  for SF<sub>6</sub> at p = 90 Torr and for E/N < 160 Td are close to those obtained in Ref. [5] by a different technique. For pressures p = 60 Torr typical of HF lasers, the recombination coefficient in a decaying plasma is  $\beta = 4.3 \times 10^{-8}$  cm<sup>3</sup> s<sup>-1</sup> in the SF<sub>6</sub>:C<sub>2</sub>H<sub>6</sub> = 10:1 mixtures. Calculations [4] show that a decrease in the ion concentration by an order of magnitude occurs over a time ~ 200 ns comparable with the duration ~ 300 ns of the entire discharge. This leads to the assumption that ion-ion recombination in  $SF_6 - C_2H_6$ mixtures may considerably limit the ion concentration at the stage of self-sustained discharge, and should be taken into account in the calculations of the HF-laser characteristics. The simulation of the SVD in SF<sub>6</sub> using the value  $\beta = 10^{-8}$  cm<sup>3</sup> s<sup>-1</sup> for the recombination coefficient shows that in this case, the ion-ion recombination also may considerably affect the ion density balance at all stages of the discharge.

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