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# Adiabatons in the nonstationary double resonance on degenerate quantum transitions

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Abstract. The nonstationary double resonance is numerically simulated in the  $\Lambda$ -scheme of degenerate energy levels with the quantum number  $J$  of the total angular momentum equal to 0, 2, and 1. The analysis is performed in the slowly varying envelope approximation taking into account the inhomogeneous broadening of quantum transition lines. In the case of a high-power input low-frequency pulse of long duration with a flat top switched on before the application of a comparatively weak and short input high-frequency pulse and switched off after the end of the latter, a specific pulsed structure, the so-called double adiabaton, can appear. It differs from an adiabaton known from the theory of electromagnetically induced transparency by the decomposition of the high-frequency pulse into two pulses with oppositely directed elliptic polarisations.

Keywords: degeneracy of energy levels, elliptic polarisation of radiation, inhomogeneous broadening, adiabaton.

## 1. Introduction

A double resonance in laser éelds is the resonance interaction of two laser radiations with two quantum transitions sharing an energy level. The study of a nonstationary double resonance in the éelds of short pulses has revealed a number of pulsed structures such as simultons [\[1, 2\],](#page-5-0) Raman solitons [\[3\],](#page-5-0) and pulses with complete energy transfer from one pulse to another [\[4\].](#page-5-0) Extensive investigations of the phenomenon of electromagnetically induced transparency (EIT), which is a particular case of the double resonance, included the description of pulsed structures such as consistent pulses [\[5\], ad](#page-5-0)iabatons [\[6\],](#page-5-0) super-slow pulses [\[7\],](#page-5-0) and dark polaritons [8]. The use of such pulsed structures opens up new possibilities for the development of a quantum memory  $[9-11]$  and controlling laser radiation parameters  $[12-14]$ .

Theoretical studies of the nonstationary double resonance were based, as a rule, on the model of quantum transitions involving nondegenerate energy levels. Such an approach excludes effects related to a change in the polar-

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isation state of pulses during their propagation. The nonstationary double resonance on degenerate quantum transitions was studied in paper[s \[15, 16\]. B](#page-5-0)y using the method of inverse scattering problem, the authors of these papers found solutions of the simulton type for the system of equations describing this process.

The aim of our paper is to simulate numerically effects appearing in the nonstationary double resonance on degenerate energy levels taking into account a possible change in the polarisation states of interacting radiations. Unlike studies [\[15, 16\],](#page-5-0) we take into account the inhomogeneous broadening of quantum transition lines and the inequality of their oscillator strengths at which the system of evolution equations cannot be integrated by the method of inverse scattering problem [\[15\].](#page-5-0) It is assumed that energy levels are characterised in the order of their increasing energy by the quantum numbers  $J = 0, 2, 1$  of the total angular momentum operator, the upper level being shared by two resonantly excited quantum transitions (the  $\Lambda$  interaction scheme). Irreversible relaxation processes are neglected. It is assumed that a high-power low-frequency input radiation pulse of long duration with a flat top is switched on before the application of a comparatively weak and short high-frequency input pulse and is switched off after the end of the latter. Simulations are performed for the  $\Lambda$ -scheme of energy levels of the 202Pb isotope, in which EIT was observed for circularly polarised laser fields  $[17]$ . This A-scheme was chosen for the theoretical analysis due to its simplicity and the possibility of experimental verification of the obtained results. This study is a continuation of investigations [\[18\] i](#page-5-0)n which the input low-frequency radiation was weaker than the input high-frequency radiation.

## 2. Formulation of the boundary-value problem

The three-level  $\Lambda$ -scheme, consisting of the nondegenerate  $(J = 0)$  lower, five-fold degenerate  $(J = 2)$  middle, and triply degenerate  $(J = 1)$  upper levels, is formed, for example, by the  $6p^2$  <sup>3</sup>P<sub>0</sub>,  $6p^2$  <sup>3</sup>P<sub>2</sub>, and  $6p^2$  <sup>3</sup>P<sub>1</sub><sup>0</sup> levels of the <sup>208</sup>Pb isotope. Let  $M$  be the quantum number of the operator of the projection of the total angular momentum on the  $z$  axis, and  $\phi_k$  ( $k = 1, 2, ..., 9$ ) be the orthonormalised set of the common eigenfunctions of the Hamiltonian and operators of the total angular momentum and its projection on the z axis for an isolated atom, which correspond to the lower  $(k = 1, M = 0)$ , upper  $(k = 2, 3, 4, M = -1, 0, 1$ , respectively) and middle ( $k = 5, 6, ..., 9, M = -2, -1, 0, 1, 2$ , respectively) levels. Let  $D_1$  and  $D_2$  be the reduced electric dipole moments for the  $J = 0 \rightarrow J = 1$  and  $J = 2 \rightarrow J = 1$  transitions, respec-

We represent the electric field of two laser pulses propagating along the z axis with carrier frequencies  $\omega_1$  and  $\omega_2$ in the form

$$
E = \sum_{l=1}^{2} \mu_l [iE_{xl} \cos(\omega_l t - k_l z + \delta_{xl})
$$

$$
+ jE_{yl} \cos(\omega_l t - k_l z + \delta_{yl})],
$$
(1)

where  $\mu_l = h\sqrt{2l+1}/(|D_l|T_1)$ ; i and j are the unit vectors of the x and y axes;  $E_{xl}$ ,  $E_{vl}$ ,  $\delta_{xl}$ ,  $\delta_{vl}$  are functions of z and t; and  $k_1 = \omega_1/c$ . Because  $\omega_1 > \omega_2$ , radiation at frequency  $\omega_1$ is the high-frequency radiation, while radiation at frequency  $\omega_2$  is the low-frequency radiation.

The wave function of an atom can be written in the form

$$
\Psi = \bar{c}_1 \phi_1 + \left(\sum_{k=2}^4 \bar{c}_k \phi_k\right) \exp(-i\xi_1)
$$

$$
+ \left(\sum_{k=5}^9 \bar{c}_k \phi_k\right) \exp\left[-i(\xi_1 - \xi_2)\right],
$$
 (2)

where  $\xi_l = \omega_l t - k_l z$ . Let us introduce variables  $f_l$  and  $g_l$ and quantities  $c_i$ :

$$
f_l = [E_{xl} \exp(i\delta_{xl}) - iE_{yl} \exp(i\delta_{yl})] / \sqrt{2},
$$
  
\n
$$
g_l = [E_{xl} \exp(-i\delta_{xl}) - iE_{yl} \exp(-i\delta_{yl})] / \sqrt{2},
$$
  
\n
$$
c_1 = -2\bar{c}_1 \arg D_1, \ c_2 = \bar{c}_2, \ c_4 = \bar{c}_4, \ c_5 = 2\bar{c}_5 \arg D_2,
$$
  
\n
$$
c_7 = (2/\sqrt{6})\bar{c}_7 \arg D_2, \ c_9 = 2\bar{c}_9 \arg D_2.
$$

Let us define the normalised independent variables s and w as

$$
s = z/z_0, \ w = (t - z/c)/T_1,
$$
 (3)

where  $z_0 = 3\hbar c/(2\pi N |D_1|^2 T_1 \omega_1)$  and N is the concentration of atoms. By describing the evolution of the éeld and atoms with the help of Maxwell and Schrödinger equations, respectively, we obtain, in the slowly varying amplitude approximation, the system of equations

$$
\frac{\partial f_1}{\partial s} = \frac{i}{\sqrt{\pi}} \int_{-\infty}^{+\infty} c_1 c_2^* \exp(-\varepsilon_1^2) d\varepsilon_1,
$$
  

$$
\frac{\partial f_2}{\partial s} = -\frac{i}{\sqrt{\pi}} \xi \int_{-\infty}^{+\infty} (c_4^* c_9 + c_2^* c_7) \exp(-\varepsilon_1^2) d\varepsilon_1,
$$
  

$$
\frac{\partial g_1}{\partial s} = \frac{i}{\sqrt{\pi}} \int_{-\infty}^{+\infty} c_1^* c_4 \exp(-\varepsilon_1^2) d\varepsilon_1,
$$
  

$$
\frac{\partial g_2}{\partial s} = -\frac{i}{\sqrt{\pi}} \xi \int_{-\infty}^{+\infty} (c_2 c_5^* + c_4 c_7^*) \exp(-\varepsilon_1^2) d\varepsilon_1,
$$

$$
\frac{\partial c_1}{\partial w} = -i(f_1c_2 - g_1^*c_4),
$$
\n
$$
\frac{\partial c_2}{\partial w} + i\varepsilon_1 c_2 = -\frac{i}{4}(f_1^*c_1 + g_2c_5 - f_2^*c_7),
$$
\n
$$
\frac{\partial c_4}{\partial w} + i\varepsilon_1 c_4 = \frac{i}{4}(g_1c_1 - g_2c_7 + f_2^*c_9),
$$
\n
$$
\frac{\partial c_5}{\partial w} + i\varepsilon_1 (1 - \beta)c_5 = -i g_2^*c_2,
$$
\n
$$
\frac{\partial c_7}{\partial w} + i\varepsilon_1 (1 - \beta)c_7 = \frac{i}{6}(f_2c_2 - g_2^*c_4),
$$
\n
$$
\frac{\partial c_9}{\partial w} + i\varepsilon_1 (1 - \beta)c_9 = i f_2c_4.
$$
\n(4)

Here,

$$
\varepsilon_1 = T_1(\omega'_1 - \omega_1); \ \beta = \frac{\omega_2}{\omega_1}; \ \xi = \frac{3 \omega_2 |D_2|^2}{5 \omega_1 |D_1|^2}.
$$

The amplitudes  $\bar{c}_3$ ,  $\bar{c}_6$ , and  $\bar{c}_8$  do not enter into system (4). Their evolution is determined by the closed system of three differential equations, which for the initial conditions  $\bar{c}_3 = \bar{c}_6 = \bar{c}_8 = 0$ , has the trivial solution  $\bar{c}_3 = \bar{c}_6 = \bar{c}_8 = 0$ for all  $s$  and  $w$ . Integrals in the right-hand sides of the first four equations of system (4) are introduced to take into account the Doppler broadening by averaging the dipole moments of individual atoms over the parameter  $\varepsilon_1$ , which is uniquely related to the thermal velocity of each atom directed along the  $z$  axis. For the chosen transitions of the  $208Pb$ isotope, according to [\[19\],](#page-5-0)  $\beta = 0.7$  and  $\xi = 2.11$ .

The use of the plane wave approximation in our paper is justified by the fact that in most experiments on the nonstationary double resonance the laser beams of comparatively low intensity with rather large cross sections are employed. For example, it is in this approximation that all the main results of the EIT theory were obtained [\[20\].](#page-5-0) The slowly varying amplitude approximation assumes the use of long enough laser pulses so that the values of  $E_{xl}$ ,  $E_{vl}$ ,  $\delta_{xl}$ ,  $\delta_{vl}$ , and  $\bar{c}_k$  weakly change during the light oscillation cycle and over the light wavelength [\[21, 22\].](#page-5-0) We took all these factors into account in our dimensional estimates in Section 4.

Let us analyse the solutions of system (4) in terms of parameters  $a_l$ ,  $\alpha_l$ , and  $\gamma_l$  of the polarisation ellipses (PEs) of high-frequency  $(l = 1)$  and low-frequency  $(l = 2)$  radiations. Here,  $a_l$  is the major semiaxis of the PE measured in the units of  $\mu_i$ ;  $\alpha_i$  is its inclination angle to the x axis;  $\gamma_i$  is the compression parameter; and  $a_l \geq 0$ ,  $0 \leq \alpha_l < \pi, -1 \leq \gamma_l \leq 1$ [\[23\].](#page-5-0) The parameter  $|\gamma_l|$  in the ratio of the minor PE axis to its major axis, and the condition  $0 < \gamma_l < 1$  ( $-1 < \gamma_l < 0$ ) corresponds to the right-hand (left-hand) elliptic polarisation, while  $\gamma_l = 0$  corresponds to linearly polarised radiation. By specifying  $a_l$ ,  $\alpha_l$ ,  $\gamma_l$  and one of the phases, for example  $\delta_{xl}$ , we can uniquely determine the values of  $f_l$  and  $g_l$ . The parameters of the PE are generally the functions of  $s$  and  $w$ , which vary slowly over the temporal and spatial periods of the carrier quasi-harmonic.

For  $|\gamma_l| = 1$  (circular polarisation), the angle  $\alpha_l$  is not defined. The unavoidable small errors in the calculation of  $\gamma_l$ for  $|\gamma_l| \approx 1$  lead to considerable errors in the determination

of  $\alpha_l$ . To avoid these errors, we ascribed to  $\alpha_l$  the value outside the interval  $0 \le \alpha_l < \pi$ , namely, assuming that  $\alpha_l =$  $-0.1$  when  $|\gamma_l| > 0.99$ , i.e. when the PE transforms virtually to a circle. Therefore, the appearance of the negative value of  $\alpha_l$  in the dependences means the uncertainty of the angle  $\alpha_l$  at the instant when radiation is circularly polarised. If polarisation was elliptic before this moment, the angle  $\alpha_l$ changes jump-wise from a value lying in the interval  $0 \le \alpha_l < \pi$  to  $\alpha_l = -0.1$ . The jump-wise change of  $\alpha_l$  from  $\alpha_l = -0.1$  to  $0 \le \alpha_l < \pi$  occurs when circular polarisation transforms to circular polarisation. If the rotating major axis of the PE coincides with the  $x$  axis and continues its rotation in the same direction, the angle  $\alpha_l$  experiences a jump by  $\pm \pi$ . The sign of the jump depends on the rotation direction.

The initial conditions ( $w = 0$ ) for system (4) are specified in the form

$$
c_1/2 = 1, c_2 = c_4 = c_5 = c_7 = c_9 = 0, s \ge 0,
$$

which corresponds to the state in which all the atoms occupy the lower energy level at the initial instant of time. The boundary conditions  $(s = 0)$  are

$$
\alpha_l = \alpha_{l0}, \ \gamma_l = \gamma_{l0}, \ \delta_{xl} = 0, \ a_l = a_{l0}(w), \ w \ge 0,
$$
 (5)

where  $l = 1, 2$  and  $\alpha_{l0}$  and  $\gamma_{l0}$  are constants. Equalities (5) correspond to input laser pulses with a fixed orientation of the major axis and constant eccentricity of the PE, whereas functions  $a_{10}(w)$  determine the time evolution of the major semiaxis of this ellipse for high-frequency  $(l = 1)$  and lowfrequency  $(l = 2)$  pulses at the input to the resonance medium.

As additional radiation parameters, we use below the fluence  $I_l$  of high-frequency ( $l = 1$ ) and low-frequency ( $l = 2$ ) pulses measured in the units of  $c\mu_1^2/(8\pi)$  and their energy  $W_l$ per unit cross section measured in the units of  $c\mu_1^2T_1/(8\pi)$ . Below, for brevity the quantity  $W_l$  is simply called energy.

According to the theory of self-induced transparency (SIT) on nondegenerate levels, a bell-shaped pulse decays in a medium if its 'area' satisfies the condition  $\Theta_1 < \pi$  [\[24\].](#page-5-0) In the case of SIT on the degenerate  $J = 0 \leftrightarrow J = 1$  transition [\[25\],](#page-5-0) this condition is valid when the area of the input bell-shaped elliptically polarised pulse is defined by the expression

$$
\Theta_1 = \int_{-\infty}^{+\infty} a_{10}(w) \sqrt{1 + \gamma_{10}^2} \, \mathrm{d}w. \tag{6}
$$

For linearly and circularly polarised radiations, expression (6) in the case of the bell-shaped dependence  $a_{10}(w)$  coincides with the pulse area in the theory of SIT on a nondegenerate quantum transition.

#### 3. Results of calculations

3.1. Let us set in (5)

$$
\alpha_{10} = 0.5, \gamma_{10} = 0, a_{10} = 0.8 \text{ sech}(w - 7),
$$
  
\n $\alpha_{20} = -0.1, \gamma_{20} = -1,$   
\n $a_{20} = 2.46 \{\tanh[(w - 6)/2] + \tanh[(-w + 54)/2]\}.$ 

off after the end of the latter. Such an order in the application of input pulses is called the contraintuitive sequence in the EIT theory [\[6\],](#page-5-0) high-frequency and low-frequency radiations being called probe and controlling radiations, respectively. The low-frequency pulse intensity in the region of its flat top is in this case 25 times higher than the maximum intensity of the high-frequency pulse.

The dependences  $I_1(w)$  and  $I_2(w)$  are presented in Fig. 1 for different distances s. Because changes of  $I_2$  during the propagation of low-frequency radiation in a medium are comparatively small and are manifested only in the upper part of the curve, the dependences for  $I_2$  are presented in the region  $I_2 \geq 11$ .

The calculation showed that the high-frequency pulse decomposes in the medium into two separate pulses [pulses ( $1$ ) and ( $2$ ) in Figs. 1b-d]. In this case, the high-frequency radiation energy weakly decreases during propagation, approximately 1.5 times at a distance of  $s = 30$ . Note that if highfrequency radiation were absent, then, as follows from calculations, the high-frequency pulse energy for  $\theta_1 = 0.8\pi$  at this distance would decrease almost by a factor of 800.

The evolution of the PE parameters for the high-frequency pulse at a distance of  $s = 30$  is shown in Fig. 2. According to the dependence of  $a_1$ , the high-frequency pulse decomposes into pulses  $(1)$  and  $(2)$  corresponding to pulses  $(1)$  and  $(2)$  in Fig. 1d. Between these pulses, weak short closely spaces pulses are located, and pulse  $(2)$  is followed by another weak and long pulse. (These weak pulses are unnoticeable at the scale of Fig. 1d.)

In the region of pulse (1), we have  $\gamma_1 = 1$ . This means that after the decomposition of the input low-frequency pulse into component pulses, which occurs, as follows from Fig. 1, for  $s > 7$ , the first pulse has the right-hand circular polarisation. Recall that the input high-frequency pulse is linearly polarised. The value of  $\gamma_1$  in the region of pulse (2) is close to  $-1$ , as in the region of the third pulse. Therefore, pulse  $(2)$  and the third pulse have in fact left-hand circular polarisations. During each weak pulse located between



Figure 1. Evolution of the intensities  $I_1$  (thin curves) and  $I_2$  (thick curves) of high-frequency and low-frequency radiations, respectively, for different values of s.



Figure 2. Evolution of PE parameters for the high-frequency pulse for  $s = 30$ .

pulses  $(1)$  and  $(2)$ , polarisation changes from the left-hand circular  $(y_1 = -1)$  to the left- or right-hand elliptical. The dependence for  $\alpha_1$  shows that this angle increases jump-wise by  $\pi/2$  from 0.5 at the input plane and then, also jump-wise, returns to its value at the instants when the PE transforms to a circle ( $y_2 = -1$ ). Such a jump means the transformation of the major axis of the PE to the minor axis during the passage through the stage of circular polarisation.

We treat the pulsed structure obtained in this calculation as the complicated shape of an adiabaton in the case of elliptically polarised input radiations. Because the highfrequency pulse decomposes into two well separated pulses, this structure can be called a double adiabaton. The concept of the adiabaton was proposed in the study of the specific manifestation of EIT in the  $\Lambda$ -scheme for nondegenerate energy levels in the case of circular or collinear linearly polarised radiations. According to [\[6\],](#page-5-0) the adiabaton is a pair of high-frequency and low-frequency pulses, appearing if the intensities of input high-frequency and low-frequency radiations have the form shown in Fig. 1a. The high-frequency component of the usual adiabaton propagates in a medium without the energy loss and without changing the bell-shaped envelope. On the plateau of the low-frequency component of the adiabaton, a hump is formed, which is followed by a dip located in the region of the high-frequency component [\[6\].](#page-5-0) The leading and trailing edges of the lowfrequency component of the adiabaton and the hump on its plateau propagate at the speed of light in vacuum. The propagation velocities of the high-frequency component and the dip on the plateau of the low-frequency component are smaller, and, as the peak value of the high-frequency component, they decrease with decreasing the Rabi frequency of the low-frequency component of the adiabaton.

Returning to current calculations, note that linearly polarised high-frequency radiation ( $\gamma_{10} = 0$ ) incident on the medium can be represented by a sum of components with left- and right-hand circular polarisation. Quantum transitions excited by these components are shown in Fig. 3a by the arrows tilted to the left and right, respectively. The thick arrows in Fig. 3a indicate quantum transitions excited by highpower low-frequency radiation with the left-hand circular polarisation ( $\gamma_{20} = -1$ ).

It is reasonable to assume that the evolution of the lefthand circularly polarised component high-frequency radiation in the medium is determined by EIT in the  $\Lambda$ -scheme of levels 1, 7, 4, while the evolution of right-hand circularly polarised component – in the  $\Lambda$ -scheme of levels 1, 5, 2. In



Figure 3. Schemes of quantum transitions. The numbers to the left of horizontal straight lines are the numbers of states, the numbers at the top or bottom indicate the quantum number  $M$  of the corresponding states; (a) calculations in section 3.1, (b) calculations in section 3.2.

the first case, an adiabaton with the left-hand circularly polarised high-frequency and low-frequency components should appear, while in the second one  $-$  with the righthand circularly polarised high-frequency component and left-hand circularly polarised low-frequency component.

The low-frequency radiation fields (controlling fields in the EIT theory) in these  $\Lambda$ -schemes are identical. The moduli  $p_{52}$  and  $p_{74}$  of the electric dipole moments of these transitions satisfy the relation  $p_{52} = \sqrt{6} p_{74}$  [\[26\].](#page-5-0) Therefore, the Rabi frequency of the controlling field in the  $\Lambda$ -scheme of levels 1, 7, 4 is lower than that in the  $\Lambda$ -scheme of levels 1, 5, 2. Because of this, the left-hand circularly polarised high-frequency component of the adiabaton in the  $\Lambda$ -scheme of levels 1, 7, 4 has the smaller intensity and smaller propagation velocity than the right-hand circularly polarised highfrequency component of the adiabaton in the  $\Lambda$ -scheme of levels 1, 5, 2. Due to the difference in the velocities, the highfrequency components of adiabatons appearing in the two  $\Lambda$ -schemes are separated. This explains the two-pulse structure of high-frequency radiation obtained in calculations  $(Figs 1b - d)$ .

Note that both pulses of the high-frequency component of the adiabaton presented in Figs 1 and 2 decay during their propagation deep in the resonance medium, whereas the high-frequency pulse of the classical adiabaton [\[6\]](#page-5-0) propagates without the energy loss. This is explained by the fact that the adiabaton theor[y \[6\]](#page-5-0) is constructed assuming that the oscillator strengths of quantum transitions are identical and neglecting the inhomogeneous broadening of spectral lines.

3.2. In the case of linearly polarised input high-frequency and low-frequency pulses, the diagram of transitions has the form shown in Fig. 3b. The thick arrows correspond now to the right-hand and left-hand circularly polarised components of the input low-frequency radiation of the same intensity. It is obvious that in this case the left-hand and right-hand circularly polarised components of high-frequency radiation are under the same conditions, and a double adiabaton should not appear.

To elucidate how a double adiabaton transforms to a usual adiabaton described in [\[6\]](#page-5-0) when the polarisation of the input low-frequency radiation changes from circular to linear, we performed additional calculations with the boundary conditions

$$
\alpha_{10} = 0.5, \gamma_{10} = 0, \alpha_{10} = 0.8 \text{ sech}(w - 7), \alpha_{20} = 0.5,
$$
  
 $\alpha_{20} = 2.46\sqrt{1 + \gamma_{20}^2} \{\tanh[(w - 6)/2] + \tanh[(-w + 54)/2]\}$ 

for  $\gamma_{20} = -0.5, -0.25,$  and 0. The input high-frequency pulse and the intensity of the input low-frequency pulse in these calculations are the same as in section 3.1.

Figure 4a presents the dependences  $W_1(s)$  of the lowfrequency radiation energy for the values of  $\gamma_{20}$  indicated above and  $\gamma_{20} = -1$ . One can see that as  $|\gamma_{20}|$  decreases, the losses of the high-frequency radiation energy decrease and become minimal when both radiations are linearly polarised.

Figure 4b presents the intensities of high-frequency radiation pulses at a large distance  $(s = 30)$  for  $\gamma_{20} = -0.5$ ,  $\sim$  0.25, and 0 (the case  $\gamma_{20} = -1$  is shown in Fig. 1d). As  $|\gamma_{20}|$ decreases, the time interval between the pulses of the double adiabaton decreases, and when  $\gamma_{20} = 0$ , the high-frequency radiation is almost completely concentrated in one pulse accompanied by several weak pulses at its trailing edge. Our calculations showed that in this case the high-frequency radiation is linearly polarised ( $\gamma_1 = 0$ ) in the same direction as the low-frequency pulse. Such a high-frequency pulse is similar to the high-frequency component of the usual adiabaton on nondegenerate quantum transitions [\[6\].](#page-5-0)

The evolution of the PE parameters of the highfrequency radiation pulse at a distance of  $s = 30$  for small  $|\gamma_{20}|$  ( $\gamma_{20} = -0.25$ ) is shown in Fig. 5. The leading front of the first pulse of the double adiabaton has the right-hand elliptic polarisation ( $\gamma_{20} = 0.62$ ), while polarisation at the trailing edge of the pulse becomes left-hand elliptic, with variable  $\gamma_1$ . Recall that for  $\gamma_{20} = -1$ , the entire first pulse of the double adiabaton has the right-hand circular polarisation. In the region of the second pulse and low-intensity pulses, the trailing edge of the high-frequency pulse has mainly left-hand elliptic polarisation with variable parameter  $\gamma_1$ . At the instants when polarisation becomes circular, the major axis of the PE transforms to the minor axis (the angle  $\alpha_2$  changes jump-wise by  $\pi/2$ ).

3.3. Note that if the values of  $\gamma_{20}$  are changed to opposite, the results of calculations presented in section 3 remain also valid when the sign of  $\gamma_2$  is changed.



Figure 4. Dependences of the high-frequency radiation energy  $W_1$  on s (a) and of the high-frequency radiation intensity  $I_1$  on w for  $s = 30$  (b).



Figure 5. Evolution of the PE parameters for the high-frequency pulse for  $s = 30$ .

## 4. Dimensional estimates

Let us make estimates for the saturated vapour of the 208Pb isotope at temperature 950 K. In this case  $T_1 = 1.63 \times 10^{-10}$  s. By using the oscillator strengths for quantum transitions in the 208Pb isotope [\[19\]](#page-5-0) and the temperature dependence of the saturated vapour pressure for lead [\[27\],](#page-5-0) we obtain  $N = 3.4 \times 10^{13}$  cm<sup>-3</sup> and  $z_0 = 0.03$  cm. The quantities  $z_0$ and  $T_1$  are used as normalisation parameters on passing from the dimensional distance  $z$  and the dimensional time  $t$ to dimensionless variables  $s$  and  $w$  by expressions (3). Then, the duration of bell-shaped input pulses, specified in our calculations with the help of hyperbolic cosecant, will be approximately 0.4 ns. The exact value of the duration of the input low-frequency pulse with a flat top used in calculations is obviously insignificant. The duration of this pulse should only considerably exceed the duration of the input high-frequency pulse. Note that the value of  $z_0$  strongly depends on the absolute temperature. Thus,  $z_0 = 0.1$  cm at 900 K and 0.01 cm at 1000 K. The value of  $T_1$ , on the contrary, very weakly depends on the absolute temperature:  $T_1 = 1.68 \times 10^{-10}$  s at 900 K and  $1.59 \times 10^{-10}$  at 1000 K.

The dimensional intensities of low-frequency and highfrequency radiations (in kW cm<sup>-2</sup>,  $\bar{I}_1$  and  $\bar{I}_2$ , respectively) can be estimated from the expression  $\bar{I}_l = 1.3I_l$ ,  $l = 1, 2$ . The calculation by this expression in section 3.1 gives the maximum intensity of the input high-frequency radiation equal to 0.84 kW  $cm^{-2}$  and the intensity of the flat top of the input low-frequency radiation pulse equal to  $20.9 \text{ kW cm}^{-2}$ .

By using oscillator strengths for the 208Pb isotope [\[19\],](#page-5-0) we can easily estimate the relaxation times of the quantum transitions under study. The shortest of these times is 10 ns. Because low-frequency radiation acts on a quantum transition with initially unpopulated levels, each atom experiences perturbation only when it is simultaneously excited by lowfrequency and high-frequency pulses. The duration of this perturbation coincides with that of the low-frequency pulse. The latter, as noted above, is 0.4 ns, which means that the influence of irreversible relaxation can be neglected.

#### 5. Conclusions

We have shown that if a high-power input low-frequency pulse with a flat top and a long enough duration is applied contraintuitively on a weak bell-shaped input high-frequency pulse of small duration, an adiabaton of a new type can appear. The high-frequency component of this adiabaton <span id="page-5-0"></span>consists of two circular polarised pulses with electric-field strength vectors rotating in the opposite directions and with different propagation velocities.

These results, according to calculations, which are omitted here, remain valid for input high-frequency pulses of different shapes and durations under the condition that their spectral widths differ no more than  $2-3$  times from the spectral width of the resonance quantum transition with a higher frequency in the  $\Lambda$ -scheme under study. In this case, the duration of the input low-frequency pulse with a flat top should considerably exceed the duration of the input highfrequency radiation pulse. An increase (decrease) in the spectral width of the input high-frequency pulse leads to the increase (decrease) of distances at which the described effects can be observed.

The calculations preformed in the paper assumed that the frequency of each input pulse coincided with the central frequency of the corresponding quantum transition. The abandonment of this restriction may become the main direction of further investigations of the nonstationary double resonance of elliptically polarised pulses on degenerate quantum transitions.

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