On the temperature dependence of collisional linewidths of the 10^00-00^01 laser transition in the CO_2 molecule

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Abstract. Unsaturated absorption coefficients in pure carbon dioxide and $CO_2 - N_2$ and $CO_2 - He$ binary mixtures are measured at a pressure of 100 Torr in the temperature range of 300 – 700 K using a frequency-stabilised tunable $CO₂$ laser. The relative coefficients of collisional broadening caused by N_2 and He buffer gases and their temperature dependence are determined for the R(22) absorption line $(10^00 - 00^01$ transition) of the CO₂ molecule.

Keywords: absorption coefficient, collisional linewidth, carbon dioxide, nitrogen, helium.

1. Introduction

Almost all technological $CO₂$ lasers of any excitation type are known to operate at active-medium pressures providing homogeneous broadening of lasing lines due to the collisions of working-gas $(CO₂)$ molecules with other atoms and molecules of the active medium $[1-4]$.

The dependence of the collisional width Δv_{CO_2} (FWHM) of a spectral line of the $CO₂$ molecule on the gas temperature T is generally described by the formula [5]

$$
\Delta v_{\text{CO}_2} = \gamma_{\text{CO}_2-\text{CO}_2} p_{\text{CO}_2} (300 \text{ K}/T)^n, \tag{1}
$$

where $\gamma_{\text{CO}_2-\text{CO}_2}$ is the collisional linewidth related to the c[o](#page-3-0)llisions between $CO₂$ molecules at a press[ure](#page-3-0) of 1 Torr and temperature of 300 K (collisional self-broadening coefficient for the CO_2 molecule) and p_{CO_2} is the carbon dioxide pressure. The exponent *n* in (1) depends on the mechanism of interaction between colliding molecules; for the $10^0 - 00^0$ transition lines it ranges from 0.5 to 1 $[5 - 12]$.

It is also known that the main components of active media in highly efficient technological $CO₂$ lasers are carbon dioxide, nitrogen, and helium in different ratios, at pressures corresponding to the dominance of binary collisions [between](#page-3-0) atoms and molecules [1]. Therefore, the total

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collisional width $\Delta v_{\rm g}$ of the gain line profile under these conditions can be presented as the sum of contributions to broadening from pair collisions between the major-component atoms and molecules, i.e., in the form

$$
\Delta v_{\rm g} \approx \Delta v_{\rm CO_2} + \Delta v_{\rm N_2} + \Delta v_{\rm He},\tag{2}
$$

where $\Delta v_{\rm N_2}$ and $\Delta v_{\rm He}$ are the widths related to the collisions of $CO₂$ molecules with buffer N₂ molecules and He atoms, respectively.

Numerical estimates of the gain linewidth in these $CO₂$ lasers for the strongest 00^0 1 – 10^0 0 lasing transition are generally based on the formula obtained in $[13]$ for the $P(20)$ line of this transition:

$$
\Delta v_{\rm g} = \gamma_{\rm CO_2-CO_2} (\xi_{\rm CO_2} + b_{\rm N_2} \xi_{\rm N_2} + b_{\rm He} \xi_{\rm He}) p_{\Sigma} \sqrt{300/T}, \tag{3}
$$

where ξ_{CO_2} , ξ_{N_2} , ξ_{He} are the CO₂, N₂, an[d He](#page-3-0) fractions in the mixture; $b_{N_2} = \gamma_{\text{CO}_2 - N_2} / \gamma_{\text{CO}_2 - \text{CO}_2} = 0.73$ and $b_{\text{He}} =$ $\gamma_{\text{CO}_2-\text{He}}/\gamma_{\text{CO}_2-\text{CO}_2} = 0.64$ are the relative collisional broadening coefficients of $CO₂$ lines for buffer gas molecules $(N₂)$ and atoms (He), respectively; and p_{Σ} is the pressure of $CO₂ - N₂ - He$ gas mixture.

The fact that the coefficients b_{N_2} and b_{H_e} enter formula (3) as constants means in essence that the temperature dependences of Δv_{CO_2} , Δv_{N_2} and Δv_{He} values from (2) are assumed to be identical, i.e., the character of spectral line broadening upon interaction of $CO₂$ molecules with collisional partners having different properties is assumed to be the same; however, this assumption contradicts the existing representations about the mechanisms of collisional line broadening [5, 6].

The collisional linewidth is generally determined either directly (by measuring the absorption line profile using a tunable radiation source) or by measuring the unsaturated absorption coefficient at one (for example, central) frequency wit[hin](#page-3-0) [the](#page-3-0) absorption line at a pressure providing a collisionally broadened profile. The precise measurement of the entire line profile of the $CO₂$ molecule is a more complex experimental problem than the single-frequency measurement of the absorption coefécient. For the lines of the $[10^00, 02^00]_{\text{I,II}} - 00^0$ transitions [3] this problem is somewhat facilitated, because one can use the resonant radiation of a frequency-stabilised $CO₂$ laser, tunable to the lines of these transitions, as the probe radiation.

The purpose of this study w[as to](#page-2-0) determine the relative collisional broadening coefficients b_{N_2} and b_{He} of the R(22) absorption line $(10^0 - 00^01$ transition) of the CO₂ molecule for N_2 molecules and He atoms, respectively, in the temper-

2. Measurement technique and discussion of results

The absorption coefficients were measured using a frequency-stabilised tunable $CO₂$ laser at the central frequency of the R(22) line of the $10^0 - 00^01$ transition in pure CO₂ (α_{CO_2}) and $CO_2 - N_2$ and $CO_2 - He$ binary mixtures (α_{CO_2-M}) with the component ratios CO_2 : M = 1:Y at pure CO_2 and binary mixture pressures (p_{Σ}) of 100 Torr, which provide Lorentzian profiles of absorption lines.

The relative collisional broadening coefficients b_M for N_2 and He buffer gases were determined from the expression

$$
\frac{\alpha_{\text{CO}_2}}{\alpha_{\text{CO}_2-M}} = 1 + Yb_M. \tag{4}
$$

The R(22) line was chosen because the contribution to the absorption coefficient at its central frequency from the absorption line of the other overlying transitions in the $CO₂$ molecule can be neglected for the pressures and temperatures under consideration.

Note also that the use of this technique excludes the errors caused by uncertainties in the spectroscopic parameters determining the measured values of absorption coefficients [14].

The experimental setup for measuring the absorption coefficients in gases according to the double-beam compensation scheme on the lasing lines of a frequency-stabilised $CO₂$ laser, tunable to the lines of the main 00^0 I – $[10^00, 02^00]$ $[10^00, 02^00]$ $[10^00, 02^00]$ _{I,II} laser transitions, was described in detail in [15, 16]. The long-term instability of the lasing frequency with respect to the lasing line central frequency, which is resonant to the central frequency of the absorption line, did not exceed ± 0.5 MHz. This allowed us to assume with high accuracy that, for the experimentally realised absorption [linewi](#page-3-0)dths, the absorption coefficients were measured at the central frequencies of absorption lines.

The error in determining the gas pressure, Δp , was ± 0.5 Torr. The gas temperature in the measuring cell was maintained with errors of ± 0.4 K (in the range of 293 K $\leq T \leq 420$ K) and ± 0.9 K (in the range of 470 K \leq $T \leq 700 K$).

The results of measuring α_{CO_2} in pure carbon dioxide at the pressure $p_{CO_2} = 100$ Torr and temperatures from 300 to 700 K are shown in Fig. 1. The measured coefficients $\alpha_{\text{CO}_2-\text{M}}$ in CO_2-N_2 and CO_2-He binary mixtures with different component ratios at the mixture pressure $p_{\Sigma} = 100$ Torr and in the same temperature range are shown in Figs 2 and 3, respectively.

For each measurement temperature, according to formula (4), we plotted the dependence of the $\alpha_{\text{CO}_2}/\alpha_{\text{CO}_2-M}$ ratio on Y. The coefficients b_{N_2} and b_{He} were determined from the slopes of the corresponding straight lines.

Figure 4 shows as an example the dependences for the $CO_2 - N_2$ mixture at the limiting temperatures (300 and 700 K). These dependences gave $b_{\text{N}_2} = 0.74 \pm 0.02$ at $T = 300$ K and 0.99 ± 0.04 at $T = 700$ K. Similar dependences for the CO_2 – He mixture are shown in Fig. 4b. According to these data, $b_{\text{He}} = 0.58 \pm 0.03$ at $T = 300$ K and 0.88 ± 0.04 at $T = 700$ K.

Figure 1. Temperature dependence of the absorption coefficient of pure $CO₂$ at a pressure of 100 Torr on the 10R(22) line.

Figure 2. Temperature dependences of the absorption coefficient of a CO_2 : $N_2 = 1$: Y gas mixture at a pressure of 100 Torr on the 10R(22) line for $Y = 0.19$ (1), 1.5 (2), 1.78 (3), 3 (4), and 4 (5).

Thus, the experimental data in Fig. 4 clearly indicate that in the temperature range under study $(300 - 700 \text{ K})$ the $\alpha_{\text{CO}_2}/\alpha_{\text{CO}_2-N_2}$ and $\alpha_{\text{CO}_2}/\alpha_{\text{CO}_2-He}$ ratios, and, therefore, the

Figure 3. Temperature dependences of the absorption coefficient of a $CO₂$: He = 1: Y gas mixture at a pressure of 100 Torr on the 10R(22) line for $Y = 1$ (1), 2 (2), 3 (3), 4 (4), and 5 (5).

Figure 4. Dependences of the ratio of absorption coefficients, $\alpha_{\text{CO}_2}/\alpha_{\text{CO}_2-M}$, on the ratio $Y = [M]/[CO_2]$ of the concentrations of binary mixture components for $M = N_2$ (a) and He (b) at temperatures of 300 (1) and 700 K (2).

coefficients b_{N_2} and b_{He} increase with increasing gas temperature.

Note that Abrams [13], who proposed formula (3), measured the linewidth P(20) of the 10^{0} 0 – 00^{0} 1 transition in pure CO_2 and in CO_2 : $N_2 = 1:1$ and CO_2 :He = 1:1 binary mixtures by optoacoustic spectroscopy only at one temperature: $T = 298$ K. The coefficients b_{N_2} and b_{He} for several lines, including [R\(22](#page-3-0)), were measured later in the temperature range of $300 - 650$ K [17] using the technique similar to that applied in the present study. At $T = 300$ K the coefficients $b_{\text{N}_2} = 0.81 \pm 0.04$ and $b_{\text{He}} = 0.70 \pm 0.04$ were measured in [17]. Although these values somewhat exceed those obtained in this study, the quantitative agreement can be considered as fairly [good](#page-3-0).

At the same time, a qualitative comparison of our results and the data of [17], i.e., a comparative analysis of the behaviour of the coefficients b_{N_2} and b_{He} with a change in temperature leads to radically different conclusions. In particular, only small variations in b_{N_2} and b_{He} were observed [17] in the temperature range studied $(300 - 650 \text{ K})$; th[us,](#page-3-0) it was concluded that these coefficients hardly changed. The character of the change in the coefficients b_{N_2} and b_{He} with temperature, observed by us, is sho[wn](#page-3-0) in Fig. 5. It can be seen that b_{N_2} barely changes up to $T \sim 550$ K, which is in agreement with the results of [17], but noticeably increases at $T > 550$ K. The coefficient b_{He} weakly depends on temperature in the range of $T = 300 - 550$ K.

Thus, our measurements unambiguously indicate that the coeffi[cients](#page-3-0) b_{N_2} and b_{He} depend (and rather differently)

Figure 5. Temperature dependences of the relative collisional broadening coefficients of the 10R(22) line of the CO_2 molecule for N_2 (1) molecules and He (2) atoms.

on temperature. This means that the widely used formula (3) is incorrect at $T > 550$ K. According to the physical meaning of expression (2), each term in the correct formula should depend on temperature in its own way, just as the rate constants of collision-induced vibrational relaxation of the 00^0 1 upper lasing level of the CO_2 molecule in pure CO_2 and in $CO_2 - N_2$ and $CO_2 - He$ binary mixtures are characterised by their own temperature dependences (see, e.g., [18]).

Active media with a content of $CO₂$ molecules much lower than that of N_2 molecules and He atoms are optimal for high-power technological electric-discharge $CO₂$ lasers, operating with fast flow of active medium. These are CO_2 CO_2 : N₂: He ≈ 1 :(5 – 22):(5 – 22) mixtures or mixtures with even a lower content of working molecules (see, for example, $[19-22]$). In these lasers the active-medium temperature corresponding to the maximum lasing power reaches $600 - 700$ K $[23 - 25]$. Simple estimates show that the collisional gain linewidths for such $CO₂$ lasers, obtained from for[mula](#page-3-0) (3) and using our results, may differ by more than 100 %.

3. Conclusions

Unsaturated absorption coefficients in pure carbon dioxide and in $CO₂ - N₂$ and $CO₂ - He$ binary mixtures for the R(22) line of the $10^0 - 00^0$ 1 transition in CO₂ molecules were measured at a total pressure of 100 Torr in the temperature range of $300-700$ K using a frequencystabilised tunable $CO₂$ laser. The relative collisional-broadening coefficients b_{N_2} and b_{He} for N_2 and He buffer gases were determined. These parameters were found to depend on gas temperature.

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